

Atomic Structure: Frequency & Wavelength Calculations

$$E = h\nu$$

$$h = 6.63 \times 10^{-34} \text{ Joules-seconds}$$

$$1 \text{ mole} = 6.02 \times 10^{23}$$

$$c = \lambda\nu$$

$$c = 3.00 \times 10^8 \text{ m/s}$$

$$1 \text{ nm} = 1 \times 10^{-9} \text{ meters}$$

1. A certain light has a frequency of $6.0 \times 10^{14} \text{ sec}^{-1}$.

(a) What is the energy of a single photon of light at this frequency?

$$E = (6.63 \times 10^{-34})(6.0 \times 10^{14}) = \boxed{3.98 \times 10^{-19} \frac{\text{Joules}}{\text{photon}}}$$

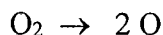
(b) What is the wavelength of this light in nanometers?

$$3.00 \times 10^8 = \lambda \cdot (6.0 \times 10^{14})$$

$$\boxed{\lambda = 5.0 \times 10^{-7} \text{ meters}}$$

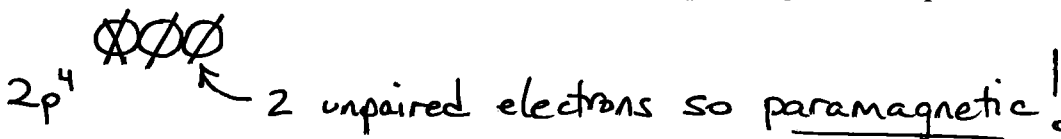
$$\frac{5.0 \times 10^{-7} \text{ meters}}{1} \times \frac{1 \text{ nm}}{1 \times 10^{-9} \text{ meters}} = \boxed{500 \text{ nm}}$$

2. The following reaction occurs in the upper atmosphere if photons having wavelengths of 240 nm and shorter strike a molecule of oxygen gas.



(a) Write the electron configuration of O. $1s^2 2s^2 2p^4$

(b) Is atomic oxygen (O) considered diamagnetic or paramagnetic? Explain.



(c) What is the electron configuration of the oxide ion, O^{2-} ? $1s^2 2s^2 2p^6$

(d) How much energy does a single photon of wavelength 240 nm possess?

$$3.00 \times 10^8 = (240 \times 10^{-9})\nu$$

$$\boxed{\nu = 1.25 \times 10^{15} \text{ sec}^{-1}}$$

$$E = (6.63 \times 10^{-34})(1.25 \times 10^{15})$$

$$\boxed{E = 8.29 \times 10^{-19} \frac{\text{Joules}}{\text{photon}}}$$

(e) How much energy does a mole of photons at 240 nm possess?

$$\left(8.29 \times 10^{-19} \frac{\text{Joules}}{\text{photon}}\right) \left(6.02 \times 10^{23} \frac{\text{photons}}{\text{mole}}\right) = \boxed{499058 \frac{\text{Joules}}{\text{mole}}}$$

$$\boxed{499 \text{ kJ/mole}}$$

3. What is the energy of a photon of radiation whose wavelength is 413 nm?

$$3.00 \times 10^8 = (413 \times 10^{-9}) \nu$$

$$\nu = 7.26 \times 10^{14} \text{ sec}^{-1}$$

$$E = (6.63 \times 10^{-34}) (7.26 \times 10^{14})$$

$$E = 4.81 \times 10^{-19} \frac{\text{Joules}}{\text{photon}}$$

4. What wavelength (in nm) of radiation has photons of energy 6.06×10^{-19} Joules?

$$6.06 \times 10^{-19} = (6.63 \times 10^{-34}) \nu$$

$$\nu = 9.14 \times 10^{14} \text{ sec}^{-1}$$

$$3.00 \times 10^8 = \lambda (9.14 \times 10^{14})$$

$$\lambda = 3.28 \times 10^{-7} \text{ meters}$$

$$3.28 \times 10^{-7} \text{ meters} \times \frac{1 \text{ nm}}{1 \times 10^{-9} \text{ meters}} = 328 \text{ nm}$$

5. A green laser pointer emits light at a wavelength of 532 nm.

(a) What is the frequency of this light?

$$3.00 \times 10^8 = (532 \times 10^{-9}) \nu$$

$$\nu = 5.64 \times 10^{14} \text{ sec}^{-1}$$

(b) What is the energy of one of these photons?

$$E = (6.63 \times 10^{-34}) (5.64 \times 10^{14})$$

$$E = 3.74 \times 10^{-19} \frac{\text{Joules}}{\text{photon}}$$

6. The energy from radiation can be used to break chemical bonds. A minimum energy of 242,000 Joules/mole is required to break a Cl-Cl bond in Cl_2 . What is the longest wavelength of radiation that possesses the necessary energy to break this bond?

$$\frac{242000}{6.02 \times 10^{23}} = 4.02 \times 10^{-19} \frac{\text{Joules}}{\text{photon}}$$

$$4.02 \times 10^{-19} = (6.63 \times 10^{-34}) \nu$$

$$\nu = 6.06 \times 10^{14} \text{ sec}^{-1}$$

$$3.00 \times 10^8 = \lambda (6.06 \times 10^{14})$$

$$\lambda = 4.95 \times 10^{-7} \text{ meters}$$

$$4.95 \times 10^{-7} \text{ meters} \times \frac{1 \text{ nm}}{1 \times 10^{-9} \text{ meters}} =$$

$$495 \text{ nm}$$